Anisotropy of the paramagnetic susceptibility in LaTiO₃: The electron-distribution picture in the ground state

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The energy-level scheme and wave functions of the titanium ions in LaTiO₃ are calculated using crystal-field theory and spin-orbit coupling. The theoretically derived temperature dependence and anisotropy of the magnetic susceptibility agree well with experimental data obtained in an untwinned single crystal. The refined fitting procedure reveals an almost isotropic molecular field and a temperature dependence of the van Vleck susceptibility. The charge distribution of the 3d-electron on the Ti positions and the principle values of the quadrupole moments are derived and agree with NMR data and recent measurements of orbital momentum $\langle l \rangle$ and crystal-field splitting. The low value of the ordered moment in the antiferromagnetic phase is discussed.

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I. INTRODUCTION

In the physics of highly correlated electron systems the electronic orbitals and their interactions are in the focus of recent experimental and theoretical research, because the orbitals play a key role in the coupling of charge and spin of the electrons with the lattice. Transition-metal oxides, where the shape and anisotropy of the d-electron orbitals determine the fundamental electronic properties, provide a rich field for this kind of investigations. For example the perovskite titanates $A \text{TiO}_3$ (with A = Y, La, or some trivalent rare-earth ion) are known as realization of a Mott insulator. The $3d^1$ electronic configuration of Ti³⁺ corresponds to an effectively half-filled conduction band, where the on-site Coulomb repulsion inhibits double occupation of the Ti-sites resulting in an insulating ground state. Although from their electronic configuration these titanates seem to be quite simple model systems, their orbital properties still have to be resolved especially in the case of $LaTiO_3$.

The debate on the orbital ground state of LaTiO₃ was triggered by its unusual magnetic properties. Below the Néel temperature $T_{\rm N}=146~{\rm K},^2$ LaTiO₃ reveals a slightly canted G–type antiferromagnetic structure with an ordered moment of $0.46\mu_{\rm B},^{3,4}$ which is strongly reduced as compared to the spin-only value of $1\mu_{\rm B}$ and, hence, indicates a strong importance of the spin-orbit coupling. On the other hand the nearly isotropic spin-wave dispersion with a small gap of about 3 meV contradicts a dominant spin-orbit coupling.⁵

This puzzling situation originates from the fact that the orthorhombic GdFeO₃ structure of LaTiO₃ deviates only weakly from the ideal cubic perovskite structure: The quasicubic crystal field of the nearly ideal oxygen octahedron surrounding the Ti³⁺ ion splits the five orbital 3d levels into a lower t_{2g} triplet and an excited e_g doublet. The single electron occupies the lower t_{2g} triplet and is Jahn-Teller active.⁶ In principle the Jahn-Teller effect is expected to lift the remaining threefold degeneracy resulting in a distortion of the oxygen octahedron in favor of one of the three orbitals. However, the competing influence of spin-orbit coupling cannot be neglected in the case of a single electron in a t_{2g} level, as has been outlined already by Goodenough⁷ and by Kugel and Khomskii.⁸ It is important to note that, as long as the orbital triplet remains degenerate, the exchange interactions are inherently frustrated even in a cubic lattice.⁹

To promote possible physics of this degeneracy in LaTiO₃, an orbital-liquid ground state has been suggested. 10 Further detailed theoretical studies 11,12 favoring the orbital-liquid picture worked out that the frustration can be resolved via an order-by-disorder mechanism giving rise to magnetic spin order with disordered orbital states. The observed spin-wave excitations were found to be in accord with this model. In a different theoretical approach^{13,14,15,16,17} the crystal field of the La ions caused by the $GdFeO_3$ -type distortion has been shown to lift the degeneracy of the $Ti-t_{2g}$ -orbitals and to stabilize the antiferromagnetic G-type order. In Ref. 13,14,15 the orbital-ground state was derived as approximately $3z_{111}^2 - r^2 = (d_{xy} + d_{yz} + d_{zx})/\sqrt{3}$. However, Solovyev¹⁷ has found that the Hartree-Fock approximation alone fails to provide the description of the magnetic properties of LaTiO₃ and YTiO₃.

Several recent experimental investigations strongly support the existence of orbital order in LaTiO₃. Specific-heat, electrical resistivity, thermal-expansion, and infrared experiments¹⁸ exhibit anomalies near the Néel temperature, which indicate significant structural changes and have been interpreted in terms of the

influence of orbital order via magneto-elastic interactions. Transmission-electron microscopy revealed small atomic displacements ascribed to a weak Jahn-Teller distortion. Detailed x-ray and neutron-diffraction studies of crystal and magnetic structure revealed an intrinsic distortion of the oxygen octahedra, which leads to a large enough splitting of the $\mathrm{Ti-}t_{2g}$ triplet state. The remeasured magnetic moment $\mu=0.57(5)\mu_{\mathrm{B}}$ turned out to be slightly larger than determined before. The reexamination of the Ti nuclear magnetic resonance spectra proves a large nuclear quadrupole splitting, which is ascribed to a rather large quadrupole moment of the 3d electrons at the Ti sites. This discarded the earlier interpretation of the NMR results in terms of orbital degeneracy and clearly favored the orbital order.

In this communication we perform a detailed analysis of the temperature dependence and anisotropy of the magnetic susceptibility of LaTiO₃, which we obtained on an untwinned single crystal. In an earlier publication²³ it was mentioned that the anisotropy observed in the paramagnetic regime requires to include the spin-orbit coupling into the crystal-field calculation. In the present analysis we develop this approach and go beyond the Hartree-Fock approximation.¹⁷ Besides the spin-orbit coupling we are taking into account the Ti–O exchange as well. We will show that the obtained orbital-order pattern is basically in agreement with NMR data²¹ and allows to describe consistently the temperature dependence and anisotropy of the observed experimental susceptibility.

II. CRYSTAL FIELD ANALYSIS

In LaTiO₃ the Ti³⁺ ions (electronic configuration $3d^1$, spin s = 1/2) are situated in slightly distorted octahedra formed by the oxygen ions. The dominant cubic component of the crystal field splits the five 3d-electron states into a lower triplet t_{2g} and an upper doublet e_g . The low-symmetry component of the crystal field is expected to be small with respect to the cubic one and, therefore, one may be tempted to analyze the magnetic susceptibility using the basis of the t_{2g} states with a fictitious orbital momentum $\tilde{l} = 1$, only.²⁴ However, this procedure is not convenient for LaTiO₃ for the following reason: Indeed, the wave functions of the fictitious momentum l=1 are defined in a local coordinate system (x, y, z) with its axes parallel to the C_4 axes of the non distorted octahedra. In the real structure of LaTiO₃, there are four different fragments TiO₆, which are distorted and rotated with respect to each other, i.e. the l=1 basis should be rotated correspondingly for each of the four inequivalent octahedra. During these rotations all 3d-electron states are mixed. In this situation it is preferable to stay in the crystallographic coordinate system using the full basis of 3d-electron states.

Thus, to determine the energy-level scheme of Ti³⁺ in

LaTiO₃, we start from the Hamiltonian

$$\mathcal{H}_0 = \xi(\mathbf{ls}) + \sum_{k=2;4} \sum_{q=-k}^{k} B_q^{(k)} C_q^{(k)}(\vartheta, \varphi). \tag{1}$$

The first term denotes the spin-orbit coupling with spin s and orbital momentum l. For Ti³+ the parameter of the spin-orbit coupling is expected to be about $\xi \approx 200$ K.²4 The second term represents the crystal field with the spherical tensor $C_q^{(k)}(\vartheta,\varphi) = \sqrt{2\pi/(2k+1)}Y_q^{(k)}(\vartheta,\varphi)$. The crystal-field parameters

$$B_q^{(k)} = \sum_j a^{(k)}(R_j)(-1)^q C_{-q}^{(k)}(\vartheta_j, \varphi_j)$$
 (2)

are calculated using available data about the crystal structure. 25,26,27 The sum runs over the lattice sites R_j .

The main contributions to the quantities $B_q^{(k)}$ originate from the point charges Z_j of the lattice and so called exchange charges. Hence, the intrinsic parameters of the crystal field are given by

$$a^{(k)}(R_j) = -\frac{Z_j e^2 \langle r^k \rangle}{R_j^{k+1}} + a_{\text{ex}}^{(k)}(R_j).$$
 (3)

The exchange contribution originates from the charge transfer from oxygen into the unfilled 3d-shell, i.e. the covalence effect, and the direct titanium-oxygen exchange coupling:^{28,29}

$$a_{\text{ex}}^{(2)}(R_j) = \frac{G}{R_j} (S_{3d\sigma}^2 + S_{3ds}^2 + S_{3d\pi}^2)$$

$$a_{\text{ex}}^{(4)}(R_j) = \frac{9G}{5R_j} (S_{3d\sigma}^2 + S_{3ds}^2 - \frac{4}{3}S_{3d\pi}^2). \tag{4}$$

Here $S_{3d\sigma}$, $S_{3d\pi}$, and S_{3ds} denote the overlap integrals for ${\rm Ti}^{3+}(3d^1)-{\rm O}^{2-}(2s^22p^6)$, which are determined in local coordinate systems with the z-axis along the titanium-oxygen bond. All integrals are calculated using the Hartree-Fock wave functions 30 of ${\rm Ti}^{3+}$ and ${\rm O}^{2-}$. The parameter G=7.2 is an adjustable parameter, which we have extracted from the cubic crystal-field splitting parameter 10Dq, which can be assumed as approximately similar for all titanium oxides, as e. g. for ${\rm Ti}^{3+}$ in ${\rm Al}_2{\rm O}_3$ with $10Dq=19000~{\rm cm}^{-1}.^{24}$

In LaTiO₃ there is no inversion symmetry at the oxygen position and, therefore, each oxygen ion exhibits a dipole moment $\mathbf{d}_i = \alpha \mathbf{E}_i$, where α denotes the polarization constant³¹ and \mathbf{E}_i is the electric field of the surrounding ions at the oxygen site with number i. For the oxygen positions^{26,27} O1 ($X=0.49036,\ 0.25,\ Z=0.07813$) and O2 ($x=0.29144,\ y=0.04116,\ z=0.71036$) at T=298 K, the values of the dipole moments (in units of $e\mathring{\mathbf{A}}$) were calculated as $d_x=-0.093,\ d_y=0,\ d_z=-0.001$ (O1) and $d_x=0.036,\ d_y=0.018,\ d_z=0.037$ (O2), respectively. The relative signs for the other three O1 and seven O2 positions change like the signs of the corresponding coordinates (X, Z, and x, y, z), e. g.

TABLE I: Contributions to the crystal-field parameters in LaTiO₃ at the Ti1 position $(\frac{1}{2}, \frac{1}{2}, 0)$ in units of K

$B_q^{(k)}$	point charges	exchange charges	dipolar
$B_0^{(2)}$	1527	720	-819
$B_1^{(2)}$	-162 - i376	-301 + i62	1548 - i413
$B_2^{(2)}$	-1229 + i2496	-941 + i103	430 + i1525
$B_0^{(4)}$	-4486	-7713	small
$B_{1}^{(4)}$	-5828 + i4105	10951 + i7733	small
$B_2^{(4)}$	11325 - i1699	19452 - i2160	small
$B_{3}^{(4)}$	1827 + i7634	3407 + i14371	small
$B_4^{(4)}$	7638 + i1713	13047 + i2963	small

TABLE II: Relative signs of the parameters $B_q^{(k)}$ for Ti2, Ti3, and Ti4 with respect to the signs for the Ti1 position in LaTiO₃

for the O1 position $(X+0.5,\,0.25,\,0.5-Z)$ we obtain $d_x=-0.093,\,d_y=0,\,d_z=0.001$ and so on. The corresponding expressions for corrections to the crystal-field parameters $B_0^{(2)},B_2^{(2)},B_1^{(2)}$ are calculated as usual.³¹

In the crystallographic coordinate system, with the Cartesian axes x, y, and z chosen along the crystal axes a=5.6071 Å, b=7.9175 Å, and c=5.6247 Å in Pnma representation (corresponding to b, c, and a in Pbnm representation, which is used in many papers), respectively, (values at room temperature 298 K) we obtain the crystal-field parameters (in K) for the titanium ion in position $\mathrm{Til}(\frac{1}{2},\frac{1}{2},0)$ as given in Table I. For the other three titanium positions the absolute values of $B_q^{(k)}$ are the same, but their signs are different (cf. Table II). Note that the quantum mechanical contributions are comparable to the classical ones and even dominate for k=4.

Using the crystal-field parameters listed above, for the position $\mathrm{Ti1}(\frac{1}{2},\frac{1}{2},0)$ we obtain the following energy spectrum of five Kramers doublets with energies $\varepsilon_{1,2}/k_{\mathrm{B}}=0$, $\varepsilon_{3,4}/k_{\mathrm{B}}=2553$ K, $\varepsilon_{5,6}/k_{\mathrm{B}}=3214$ K, $\varepsilon_{7,8}/k_{\mathrm{B}}=26773$ K, and $\varepsilon_{9,10}/k_{\mathrm{B}}=27890$ K. This excitation spectrum agrees perfectly with results from FIR experiments, which reveal a hump in the optical conductivity close to 3000 K. It is also in good agreement with the results of recent spin-polarized photo-electron spectroscopy experiments, which yield a crystal-field splitting of 0.12–0.30 eV, i.e. 1300-3300 K, of the t_{2g} subshell. The corresponding wave functions in $|m_l,m_s\rangle$ quantization are written as

TABLE III: Coefficients of the ground-state wave functions in LaTiO₃ at the Ti1 position $(\frac{1}{2}, \frac{1}{2}, 0)$

$$\begin{array}{lll} a_{m_l,m_s}^{(1)} & m_s = \uparrow & m_s = \downarrow \\ m_l = 2 & -0.479 - i0.191 & -0.033 - i0.031 \\ m_l = 1 & 0.136 + i0.025 & 0.005 - i0.020 \\ m_l = 0 & -0.032 + i0.608 & -0.011 + i0.030 \\ m_l = -1 & 0.154 - i0.047 & -0.012 - i0.007 \\ m_l = -2 & 0.526 - i0.186 & 0.048 \end{array}$$

follows:

$$|\varepsilon_n\rangle = \sum_{m_l=-2}^{+2} \sum_{m_s=\uparrow,\downarrow} a_{m_l,m_s}^{(n)} |m_l,m_s\rangle.$$
 (5)

In particular for one of the components of the ground doublet of $\mathrm{Ti1}(\frac{1}{2},\frac{1}{2},0)$ the coefficients are explicitly given in Table III. The other component of the ground state can be obtained as Kramers conjugated state. Note that the g-values $g_z=2\langle \varepsilon_1\mid k_zl_z+2s_z\mid \varepsilon_1\rangle,\ g_x=2\mid \langle \varepsilon_1\mid k_xl_x+2s_x\mid \varepsilon_2\rangle\mid$ and $g_y=2\mid \langle \varepsilon_1\mid k_yl_y+2s_y\mid \varepsilon_2\rangle\mid$ are equal for all four titanium positions, i.e. $g_z=1.81,\ g_x=1.73,\ g_y=1.79,$ where the reduction factors of the orbital momentum due to covalency have been assumed as $k_\alpha=1$. The relatively small deviation of the g value from the spin-only value 2 displays that the orbital momentum is rather small, again in agreement with the recent spin-resolved photo-emission experiments. 33

Figure 1 illustrates the orbital order pattern due to the derived ground-state wave function (cf. Table III). Basically, this is in agreement with the order patterns found by Cwik et al., 20 by Kiyama and Itoh, 21 and by Pavarini et al. 15 However, in those works the wave functions have been approximated in terms of the $t_{2g}^{(111)}$ basis only, neglecting the spin-orbit coupling.

Having obtained the orbital ground state, we are able to determine the charge distribution at the Ti sites characterized by the quadrupole moments. The tensor of the quadrupole moment per one Ti position is given by

$$Q_{\alpha\beta} = \frac{2}{21} |e| \langle r^2 \rangle \langle 3l_{\alpha}l_{\beta} - 6\delta_{\alpha\beta} \rangle. \tag{6}$$

Diagonalization of the tensors $Q_{\alpha\beta}/(|e|\langle r^2\rangle)$ calculated for all four Ti positions yields the same principal values equal to $Q_1=-0.520,\,Q_2=0.460,\,{\rm and}\,Q_3=0.060,\,{\rm i.}\,{\rm e.}$ the charge distribution on the titanium ions is the same in the local coordinate systems, which are just rotated with respect to each other. The angles of rotations have been calculated via the eigenvectors of the tensors $Q_{\alpha\beta}$. The components of the unit vectors $(n_x,\,n_y,\,n_z)$ corresponding to the principal values -0.520 and 0.460 read ${\bf n}_1=(0.815,0.573,0.086)$ and ${\bf n}_2=(-0.573,0.746,0.355)$ at the Ti1 site. For -0.520 $(0.460)\,n_y\,(n_x)$ is reversed at the Ti3 and Ti4 sites, whereas n_z is reversed at the Ti2 (Ti2) and Ti4 (Ti3) sites.

It is interesting to know, how the spin is oriented with respect to the quadrupole charge distribution. According to neutron-scattering data^{20,34} and susceptibility measurements^{4,23} the effective magnetic moment per

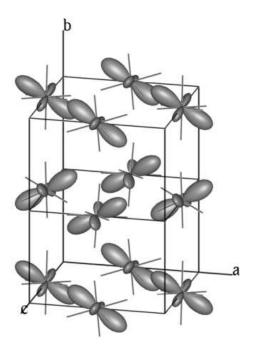


FIG. 1: Orbital order in ${\rm LaTiO_3}$ as derived from the crystal-field analysis

one ${\rm Ti}^{3+}$ is about $\mu_{\rm eff} \sim 0.6 \mu_B$. The antiferromagnetically ordered moments are aligned along the c-direction and weak ferromagnetism shows up along the b-direction (in Pnma).²⁰ We suggest that this can be explained as follows: Due to the spin-orbit coupling the orientations of the titanium magnetic moments are connected with the quadrupole ordering. If we assume that the spin is aligned perpendicular to the 3d-electron chargedistribution plane, i. e. along \mathbf{n}_2 , a ferromagnetic alignement along the b-axis can result from the y component of \mathbf{n}_2 , which is positive at all four Ti places, and a Gtype antiferromagnetic order along the c-axis is favored as the sign of the z-component of \mathbf{n}_2 changes between the Ti sites, correspondingly. As neutron scattering detects the averaged magnetic moment of the four inequivalent Ti places per unit cell with vice versa twisting of the quadrupolar moments, the observed $\mu_{\text{eff}} \sim 0.6 \mu_B$ is just the projection of the total magnetic moments onto the c-direction.

III. MAGNETIC SUSCEPTIBILITY

The LaTiO₃ single crystal, prepared by floating zone melting,² was essentially the same as used previously for the thermal-expansion measurements described in Ref. 18. The crystallographic axes were determined from x-ray Laue pictures. Additional neutron-diffraction experiments³⁴ on the same crystal revealed only a small twin-domain of about 5% of the crystal volume, hence the crystal can be regarded as practically untwinned. The magnetization M(T) was measured in a commercial

superconducting quantum interference device (SQUID) magnetometer (MPMS5, Quantum Design), working in a temperature range $1.8 \le T \le 400$ K and in magnetic fields up to H=50 kOe.

Figure 2 shows the temperature dependence of the susceptibility $\chi = M/H$ obtained from the LaTiO₃ single crystal in an external field of H = 10 kOe applied along the three orthorhombic axes both below T_N (inset) and in inverse representation in the paramagnetic regime (main frame). The data have been corrected accounting for the diamagnetic background of the sample holder, which was measured independently for all three geometries. Below the Néel temperature $T_{\rm N}=146$ K, one observes the evolution of a weak ferromagnetic magnetization of about $0.02\mu_{\rm B}$ per formula unit with its easy direction along the c-axis. The paramagnetic regime is better visible in the inverse susceptibility with an approximately linear increase above 200 K. Evaluation by a Curie-Weiss behavior $N_{\rm A}\mu_{\rm eff}^2/3k_{\rm B}(T+\Theta_{\rm CW})$, with $\mu_{\rm eff}^2=\mu_{\rm B}^2g^2S(S+1)$ yields a Curie-Weiss temperature $\Theta_{\rm CW}\approx 900$ K and an effective moment $\mu_{\rm eff} \approx 2.6 \mu_{\rm B}$, which is strongly enhanced with respect to the spin-only value of $1.73\mu_{\rm B}$. For an appropriate evaluation we have to take into account the preceding energy-level scheme derived from our CF analysis.

Including the external magnetic field, the perturbation Hamiltonian is written as

$$V = -\mu_{\rm B} H_{\alpha} (k_{\alpha} l_{\alpha} + 2s_{\alpha} - f_{\alpha} s_{\alpha}) = -H_{\alpha} M_{\alpha}. \tag{7}$$

Here the factors f_{α} take into account the molecular field, which can be anisotropic for two reasons. The first one is because of the anisotropic g-factors. The second one is due to the anisotropy of the effective superexchange interaction between the titanium spins, which we take in the form $\sum_{\alpha} J_{ij}^{\alpha} s_{\alpha}^{i} s_{\alpha}^{j}$. The parameters J_{ij}^{α} represent the effective superexchange integrals, $\alpha = x, y, z$. In the crystal structure around each Ti^{3+} ion, there are two titanium ions at a distance $\mathrm{R}_{1} = 3.958$ Å, four titanium ions at $\mathrm{R}_{2} = 3.971$ Å, and 12 at a distance $\mathrm{R}_{3} \approx 5.6$ Å. According to the neutron-scattering data⁵ $J_{1}^{\alpha} \approx J_{2}^{\alpha} \approx$

The molecular field approximation taking into account the six nearest neighbors at distances R_1 and R_2 yields

180 K for all α .

$$f_{\alpha} = \frac{6J\langle s_{\alpha}\rangle\langle k_{\alpha}l_{\alpha} + 2s_{\alpha}\rangle}{k_{\rm B}T + 6J\langle s_{\alpha}\rangle^{2}} = \frac{C_{\alpha}}{T + \Theta_{\alpha}}.$$
 (8)

Note that in this approximation the ratios $C_{\alpha}/\Theta_{\alpha}$ are independent on the exchange coupling J_{α} and directly determined by the spin- and orbital state as

$$\frac{C_{\alpha}}{\Theta_{\alpha}} = \frac{\langle \varepsilon_{1} \mid k_{\alpha} l_{\alpha} + 2s_{\alpha} \mid \varepsilon_{1} \rangle}{\langle \varepsilon_{1} \mid s_{\alpha} \mid \varepsilon_{1} \rangle}.$$
 (9)

The ratios $C_x/\Theta_x \approx 1.92$ and $C_y/\Theta_y \approx 1.85$, and $C_z/\Theta_z \approx 1.80$, as calculated from the ground state assuming $k_\alpha = 1$, indicate again an only small contribution of the orbital momentum l_α to the magnetic susceptibility. For zero orbital momentum one would obtain $C_\alpha/\Theta_\alpha = 2$.

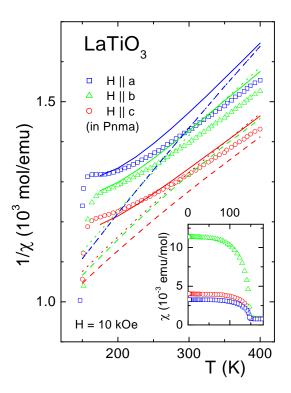


FIG. 2: Temperature dependence of the inverse susceptibility $1/\chi(T)$ (Inset: $\chi(T)$ at low temperatures) in LaTiO₃ for an external field of H=10 kOe applied along the three crystalographic axes a, b, and c (Pnma). The fits indicated by solid, dashed, and dotted lines are described in the text (color online).

For $\alpha=z$ the paramagnetic part of the susceptibility can be written as

$$\chi_{para}^{zz} = \frac{1}{Z} \sum_{l} \langle \varepsilon_l \mid M_z \mid \varepsilon_l \rangle^2 \exp(-\varepsilon_l / k_{\rm B} T)$$
 (10)

where $Z = k_{\rm B}T \sum_{l} \exp(-\varepsilon_l/k_{\rm B}T)$. The van Vleck like contribution reads

$$\chi_{\text{vv}}^{zz} = 2\sum_{l}' \frac{\langle \varepsilon_{1} \mid M_{z} \mid \varepsilon_{l} \rangle \langle \varepsilon_{l} \mid M_{z} \mid \varepsilon_{1} \rangle}{\varepsilon_{l} - \varepsilon_{1}}.$$
 (11)

The cases $\alpha=x,y$ can be written analogously. In addition, one has to take into account the diamagnetic susceptibility. It can be estimated from the ionic susceptibilities³⁵ (given in 10^{-6} emu/mol) of Sr²⁺ (-15), which is isoelectronic to La³⁺, Ti³⁺ (-9), and O²⁻ (-12) as $\chi_{\rm dia}=-6\cdot 10^{-5}$ emu/mol.

In Fig. 2 the theoretical description of the data has been performed in three steps, as illustrated by the three groups of dashed, dotted, and solid lines, respectively. In the first step (dashed lines) the exchange coupling is assumed to be isotropic and used as the only fit parameter $J_{\alpha} = J$. The reduction factors have been kept fixed at $k_{\alpha} = 1$. With J = 200 K in good agreement with the results of neutron scattering, one achieves already a reasonable description of the susceptibility. It is remarkable

that absolute value and anisotropy are very well reproduced by this straight-forward calculation.

In the second step, we allowed a variation of the covalency parameters k_{α} . With the same exchange constant of 200 K and $k_x=1$, $k_y=0.88$, and $k_z=0.95$ (dotted lines) the description of the relative splitting of the susceptibilities between the different axes is improved, but the curvature is still not reproduced. Nevertheless, the obtained covalency parameters match the values typically observed for Ti³⁺ ions.²⁴ The resulting ratios $C_{\alpha}/\Theta_{\alpha}$ change only slightly $C_x/\Theta_x \approx 1.92$ and $C_y/\Theta_y \approx 1.87$, and $C_z/\Theta_z \approx 1.81$ with respect to $k_{\alpha}=1$.

Finally in the third step, the solid lines show the fit of the experimental data using in addition the values C_{α} and Θ_{α} as adjustable parameters. From fitting we have got $C_x/\Theta_x = 2.45$, $C_y/\Theta_y = 2.29$, and $C_z/\Theta_z = 2.14$. These deviations from the nearestneighbor isotropic molecular-field results can be considered as a hint for an spin-orbit dependent exchange like $J(s_i s_j) l_{\alpha}^i l_{\beta}^j$ between the titanium ions. In principle such kind of operators are known and have been discussed in a number of papers^{36,37,38,39} in application to the susceptibility of the dimer $[\mathrm{Ti_2Cl_9}]^{-3}$ and *a-priory* cannot be discarded for LaTiO₃. Another influence, which to our opinion cannot be excluded as well, is the next nearest neighbor interaction between the titanium ions. Obviously this question should be addressed to further analysis, when more experimental information will be obtained. However, both types of mentioned interactions can produce the corrections of a few percent, but we believe that the essential physics of the temperature dependence of magnetic susceptibility and orbital ordering will be the same as described above.

Note that the factor f_{α} is quite large and, therefore, according to Eq. 11 $\chi_{\rm vv}^{\alpha\alpha}$ is dependent on temperature. This fact to our knowledge has not been pointed out in literature. We think that this situation should be quite general for other titanium compounds as well as for vanadium oxides.

IV. CONCLUSIONS

In summary the energy splitting and wave functions of the Ti^{3+} $3d^1$ —electron state have been calculated for $\mathrm{LaTiO_3}$ due to the crystal field including spin-orbit coupling and $\mathrm{Ti-O}$ exchange. From the derived orbital ground state we have estimated the quadrupole moments at the Ti sites and have deduced the charge-distribution picture for the 3d–electrons in the crystallographic coordinate system. Based on the orientation of the quadrupolar tensor, it is possible to suggest an explanation for the low value of the ordered moment, observed in the antiferromagnetic state. The straight-forward calculation of the paramagnetic susceptibility yields the correct anisotropy, which we measured in an untwinned $\mathrm{LaTiO_3}$ single crystal

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